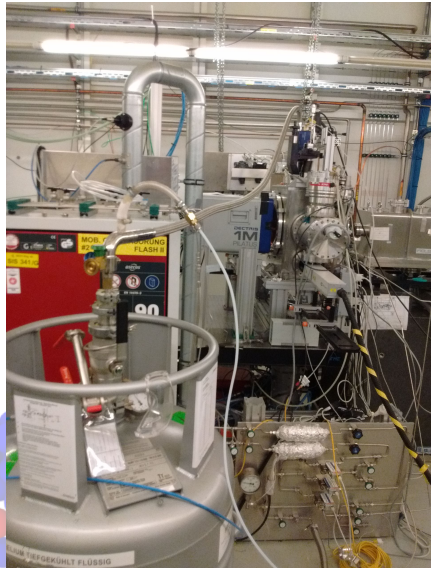
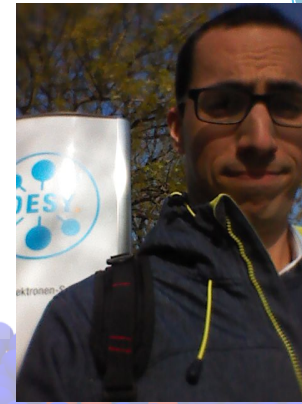


**Energy - landscape driven  
crystallization slowdown  
in supercooled liquid mixtures**

# 2015 - 2018: three experimental campaigns on supercooled Argon – Krypton liquid mixtures @ PETRAIII synchrotron source c/o DESY

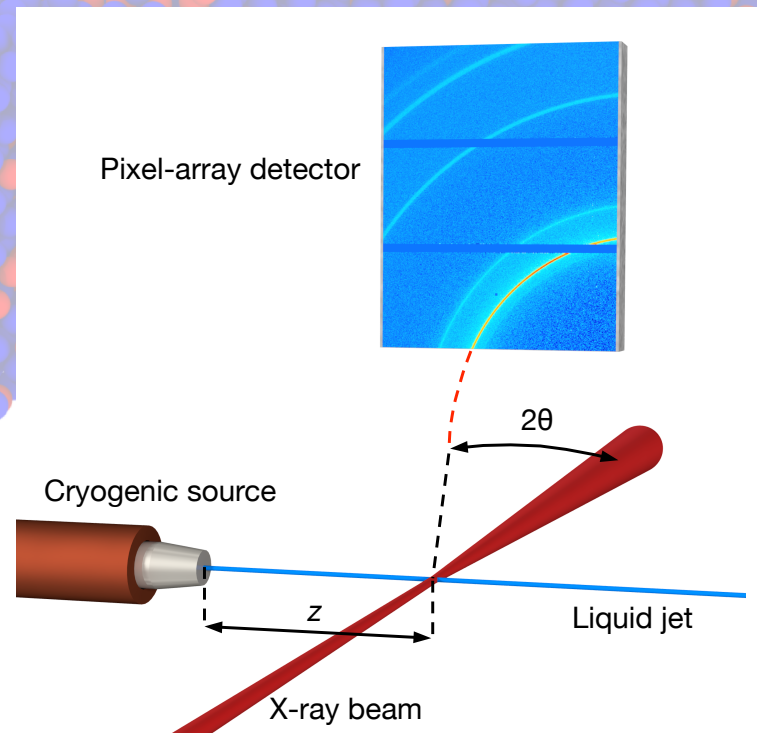


- Liquid microjets technique<sup>1</sup>
- Evaporative cooling



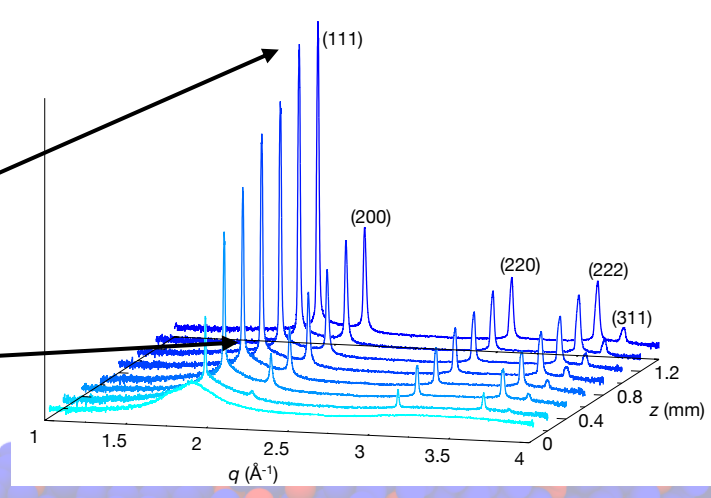
- #1 The experiment
- #2 The experiment – II
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- Distance from nozzle:  
time evolution ( $t=z/v$ ,  
 $v$  of the jet constant)
- X-rays diffraction on the  
supercooled filament

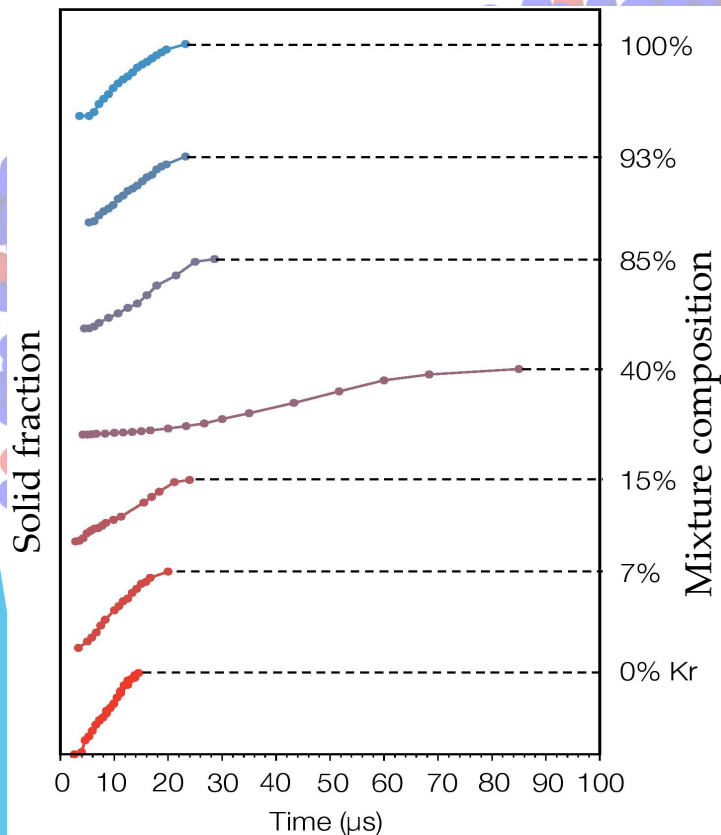


➤ Crystal growth rate extracted from the area below Bragg peaks in the static structure factor

FCC crystal peaks

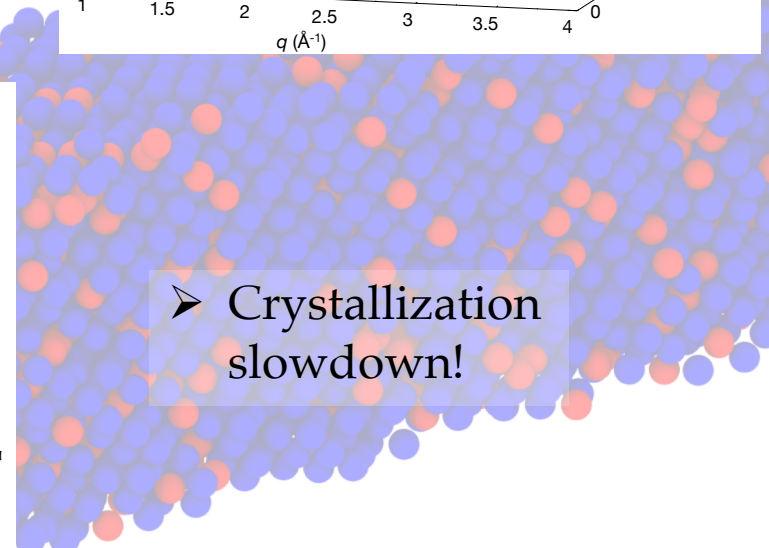


- #1 The experiment
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➤ Crystallization slowdown!

➤ Slowdown for Ar-rich and Kr-rich systems both



➤ Crystallization of supercooled liquids:  
from climate science to amorphous solids



➤ Crystallization delay observed in various simulated systems  
(binary metallic alloys<sup>1</sup>, Kob-Andersen<sup>2</sup> model...)  
+ link with **glass transition**



➤ **Why the slowdown?**

atomic size

crystal deposition rate

**Geometric frustration? Diffusion?**

$$u = f a \nu \left( 1 - e^{-\Delta G / k_B T} \right)$$

fraction of active sites

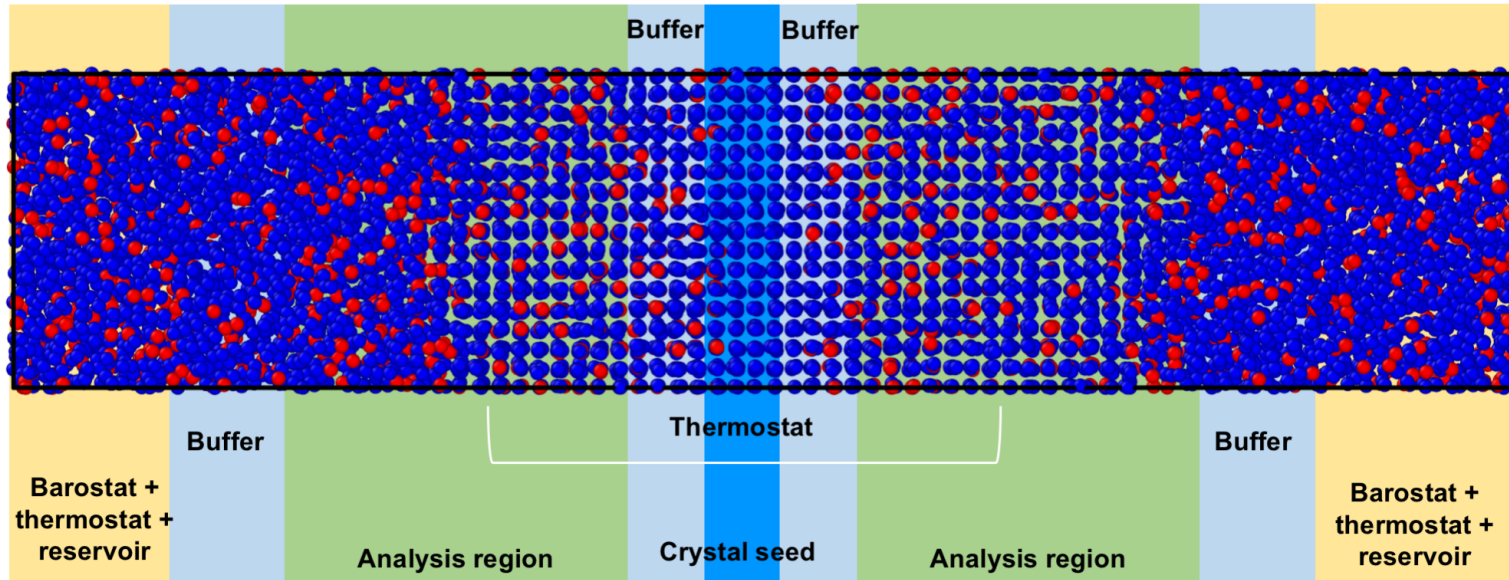
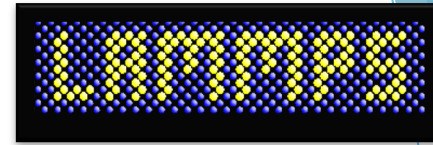
➤ Frenkel-Wilson equation  
for crystal growth rate

➤ Does this model lack the dependence on  
mixing ratio in  $\nu$ ?

- #1 The experiment
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1. Tang *et al.*, Nature Mat. (2013)  
2. Pedersen *et al.*, Phys. Rev. Lett. (2018)

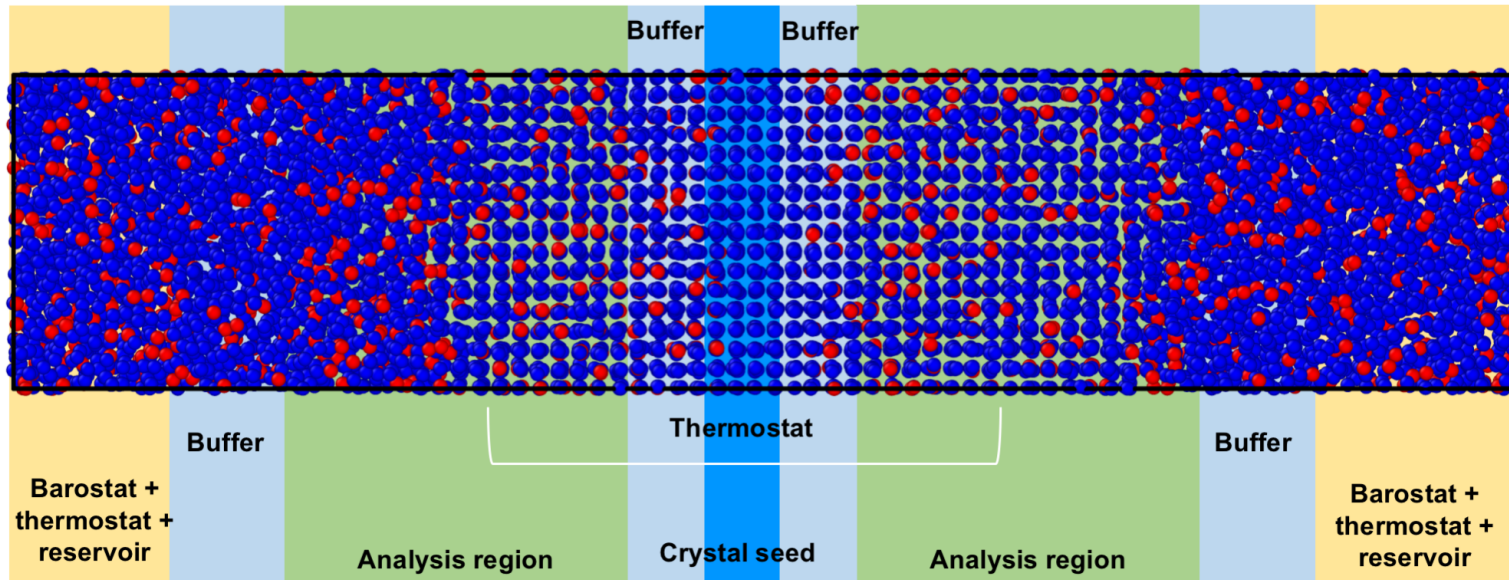
- Simulation method: Molecular Dynamics  
LAMMPS package ([www.lammps.sandia.gov](http://www.lammps.sandia.gov))



- #1 The experiment
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- Elongated box, (100) and (111) directions, from 9000 up to 21000 atoms, 3D PBC
- Realistic central crystal seed

- Uniform crystallization process → constant pressure and chemical potential <sup>1,2,3</sup>



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- barostat corrections only in external regions and along crystallization axis
- adaptive Bussi-Parrinello thermostat<sup>4</sup>

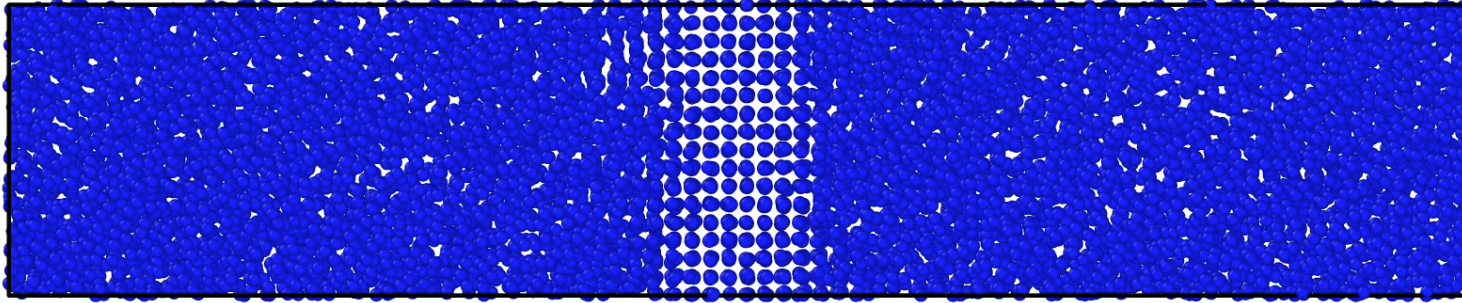
1. Perego *et al.*, J. of Chem. Phys. (2015)

2. Radu *et al.*, Phys. Rev. Lett. (2017)

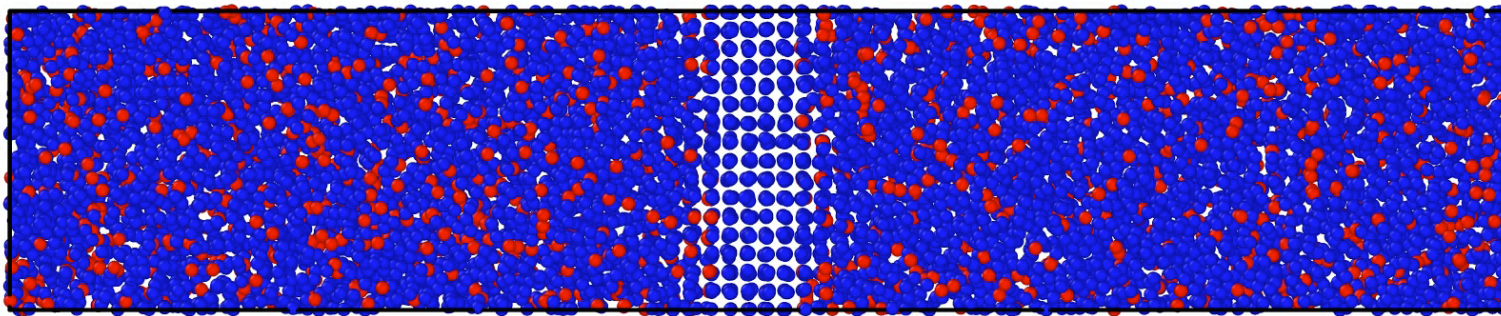
3. Tang *et al.*, Nature Mat. (2013)

4. Bussi *et al.*, J. of Chem. Phys. (2007)

100% Argon



15% Krypton - 85% Argon



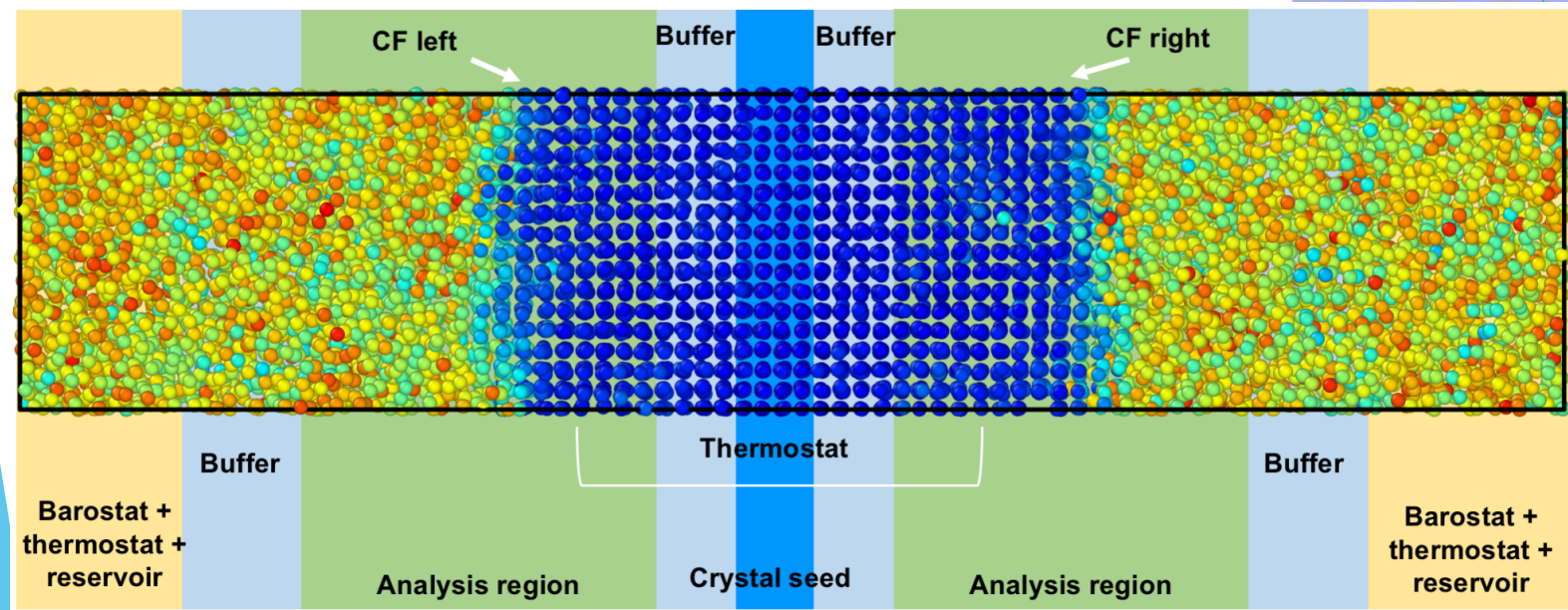
- #1 The experiment
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➤ Structural order parameter<sup>1,2</sup>

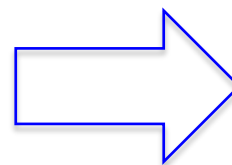


➤ Find the crystal front position

- #1 The experiment
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- #7 **Local Bond Order**
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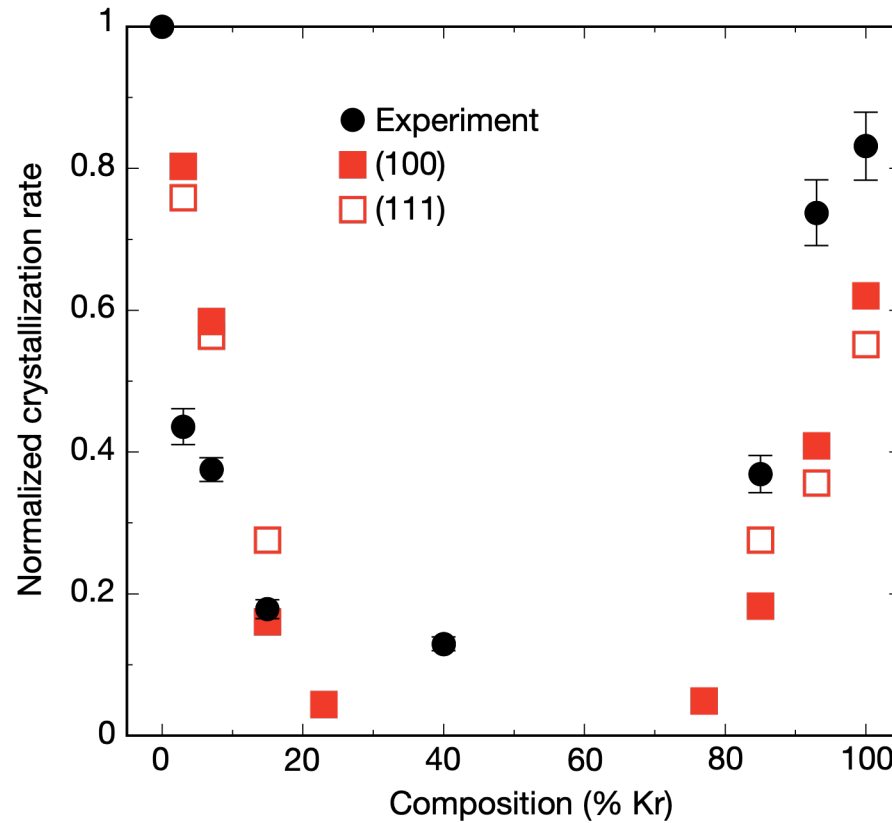
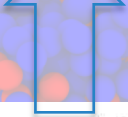
➤ velocity of the crystal front



**crystal growth rate!**

1. Steinhardt *et al.*, Phys. Rev. B (1985)
2. Lechner *et al.*, J. of Chem. Phys. (2008)



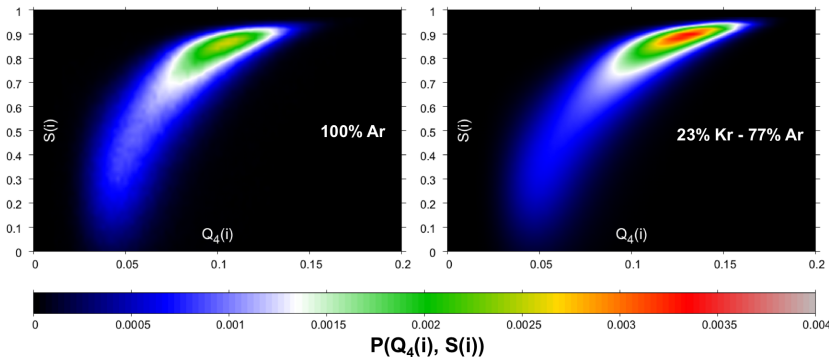


➤ Good agreement with experimental data: MD simulations capture relevant details!

Slowdown on both sides → No temperature effect!

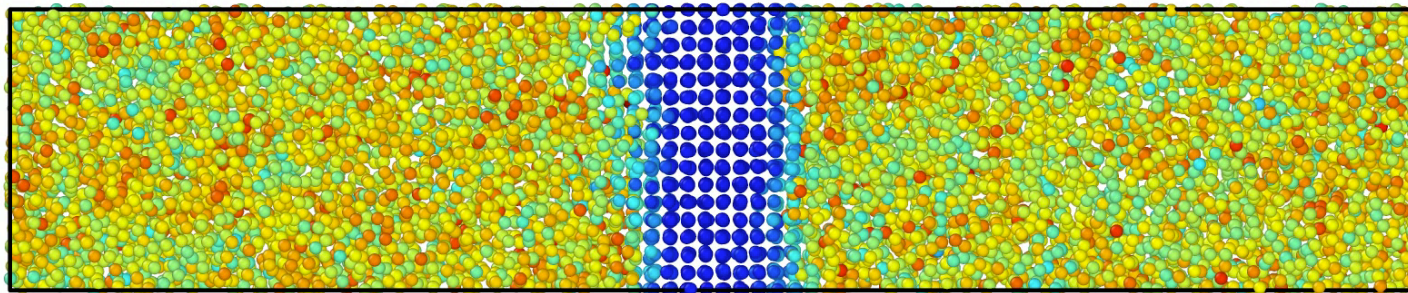
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- No icosahedra or peculiar locally favoured structures (typical reason addressed for slowdown)
- What happens at the **crystal/liquid interface**?

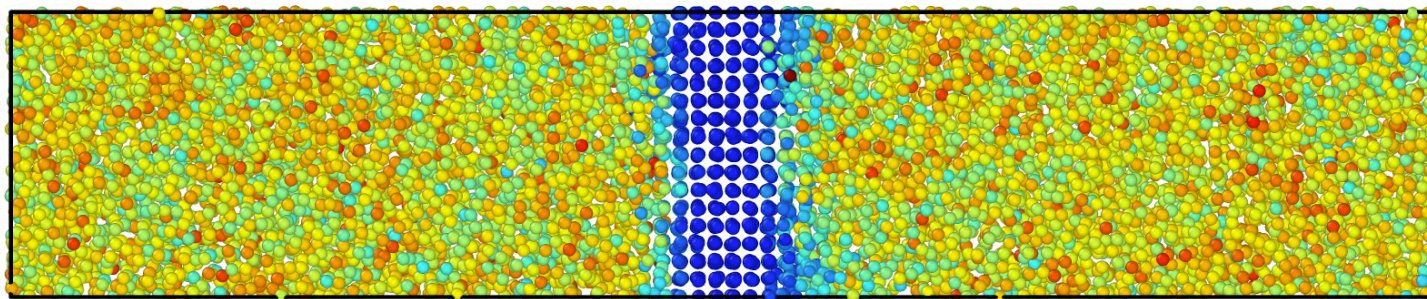


➤ Appreciable differences: crystal/liquid interface is more variegated for mixtures

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100% Ar



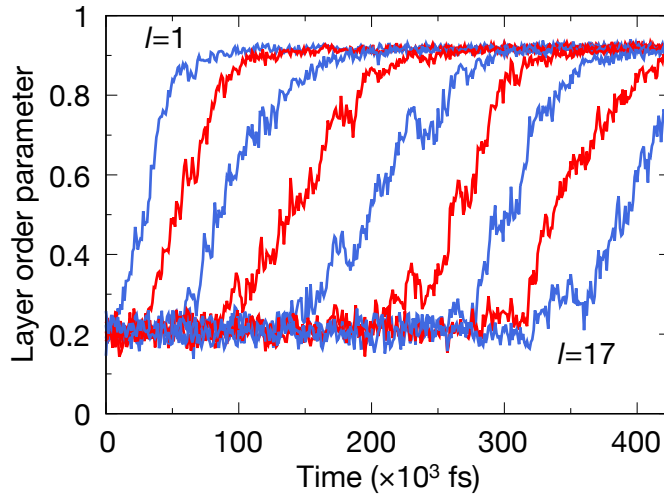
15% Kr –  
85% Ar



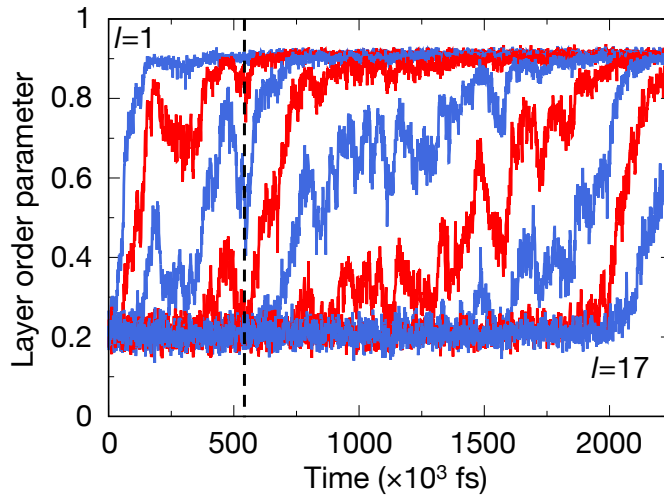
- Define the layer average of  $S(i)$ ,  $\langle S \rangle_l$
- Time evolution of  $\langle S \rangle_l$  for a pure system and a mixture

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100% Ar



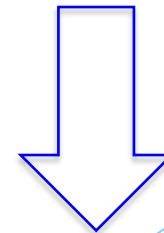
15% Kr –  
85% Ar



➤ Intrinsic slope of the  $\langle S \rangle_l(t)$  curves is almost identical

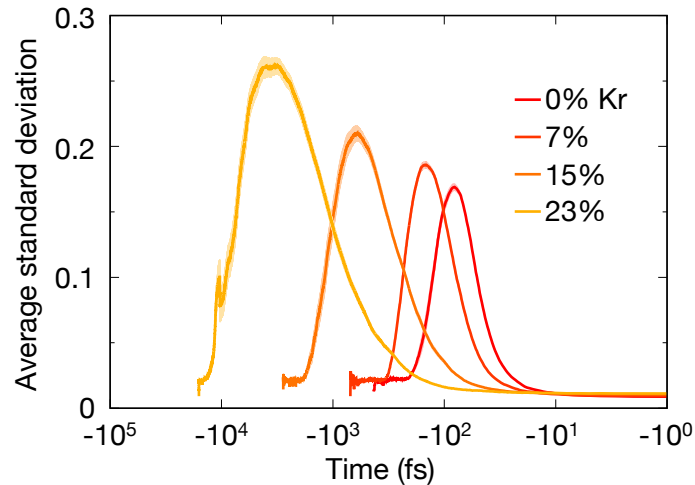
➤  $\langle S \rangle_l$  drops (different timescales!)

➤ Regression towards a more disordered state is more frequent in binary systems



➤ Microscopic explanation of the crystallization slowdown

➤ Statistical analysis of  $\langle S \rangle_1(t)$  → Standard deviation of  $\langle S \rangle_1(t)$

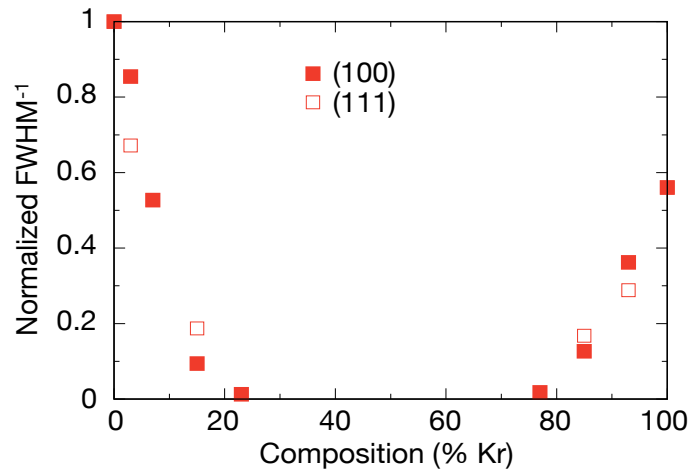


➤ Note the x-log scale

➤ Negative time: result of a time-shift to allow statistical analysis

➤ Height + width: extent of the fluctuations

➤ Striking similarity between  $\text{FWHM}^{-1}$  and crystal growth rate as a function of the composition



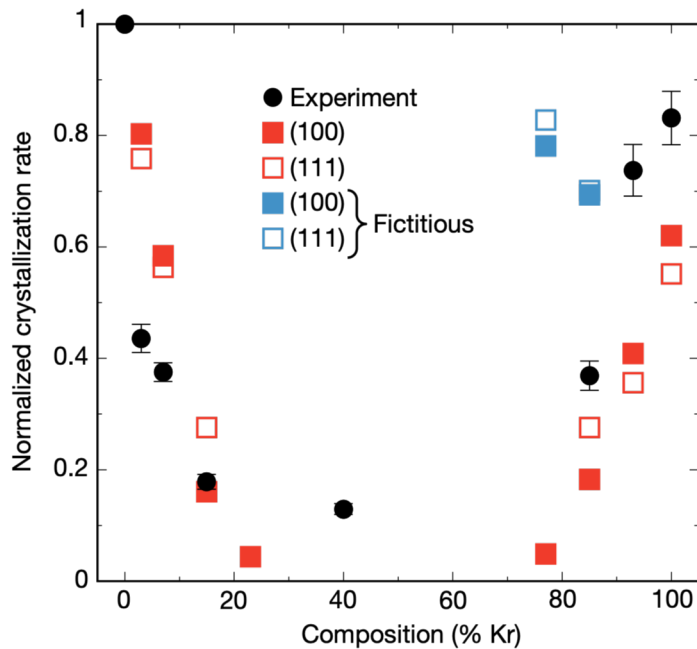
➤ Structural fluctuations between the liquid and crystal states → a fundamental feature of the mechanism of crystal growth

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- Is the dominant effect a **kinetic** or a **potential** contribution?
- Simulation of fictitious systems: distinguished masses, but Kr-Kr potential for all pairs  
→ faster crystallization kinetics (no slowdown) and the structural fluctuations decrease

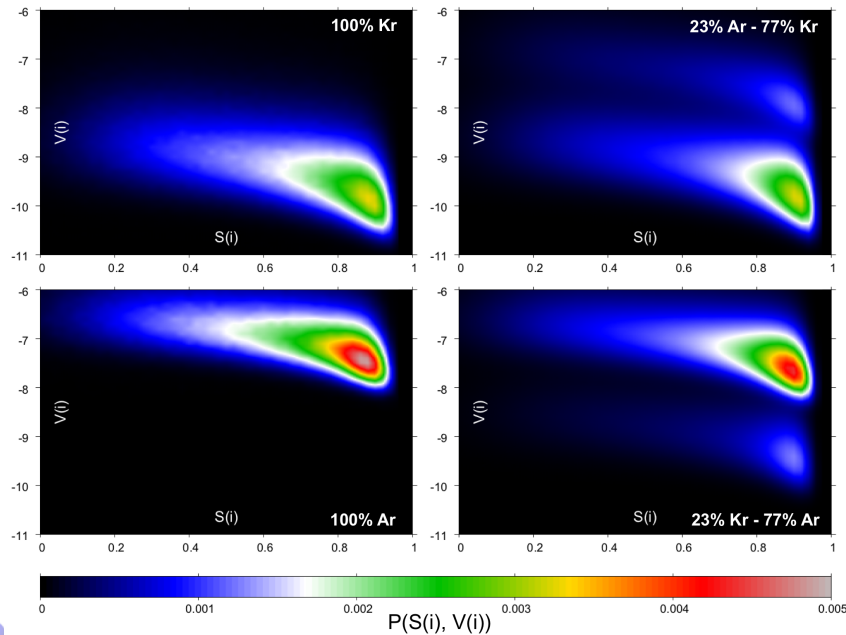
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Mass (i.e. diffusion)  
is not fundamental



- Particle size + potential depth effect  
**Potential Energy Landscape**  
relevant role

Joint probability in (S, V) plane

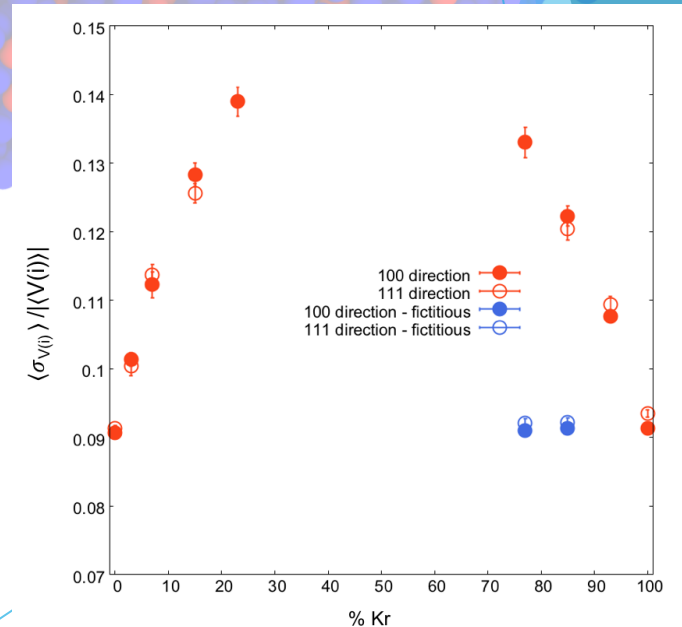


➤ Deep modifications induced in the PEL by the mixed interactions

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$$V(i) = \sum_{j(\neq i)} V_{\alpha(i)\beta(j)}(|\mathbf{r}_i - \mathbf{r}_j|)$$

- Measure of the average relative fluctuations of the potential energy at the interface for the  $i$ -th particle
- Direct link between the crystal growth rate and the modification of the PEL exploration



## Our work:

- ✓ First experiment ever on x-ray diffraction of liquid/solid filaments → real sample & ideal model for binary LJ mixtures
- ✓ Simulated & experimental crystal growth rates  
→ substantial agreement
- ✓ Fictitious systems (mass/size effects)
- ✓ Detection of  $\langle S \rangle_1(t)$  structural fluctuations  
→ slowdown microscopic origin!
- ✓ Potential energy landscape key role<sup>1</sup>

## What's next?

- How to effectively include these concepts into a more sophisticated theory of crystal growth, extending present models?
- Energy minimization at the interface<sup>2</sup>
- Free energy enhanced sampling methods
- Nucleation study
- More powerful experimental technique (XCCA)

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1. Schottelius, Mambretti *et al.*, under review in Nat. Mat. (2018)

2. Sun *et al.*, Nat. Mat. (2018)

➤ Need for HPC resources: MARCONI & GALILEO supercomputing facilities (CINECA)

- CINECA LISA 2016:  
PUMAS project

- ISCRA C 2017:  
GLEMD project

- ISCRA B 2018:  
MEMETICO project



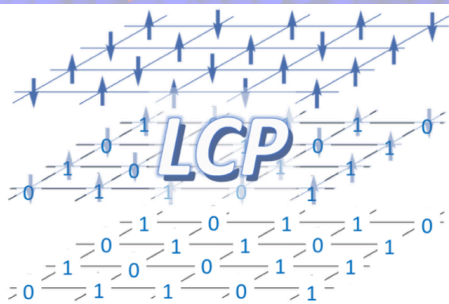
Regione Lombardia



Thanks to **Davide E. Galli**, the Milano team,  
**Robert E. Grisenti**, **Alexander Schottelius**,  
the Frankfurt team and the DESY PETRA III team

Grisenti Research Group

@ Institut für Kernphysik Frankfurt



Thanks for your time!